

**STATISTICAL ESTIMATION OF THE UNAVAILABILITY  
OF THE MNR SAFETY AMPLIFIER**

**By**

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## **ABSTRACT**

Unavailability of the McMaster Nuclear Reactor (MNR) Safety Amplifier is calculated and showed to be within acceptable limits. Treated as a system of moderate complexity, the MNR Safety Amplifier reliability parameters are studied in detail utilizing a fault tree technique. This technique is recommended by IAEA and widely adopted in nuclear engineering as a main route for performing probabilistic risk assessment. A fault tree is developed and reliability parameters are calculated using a commercial software application FaultTree+™. Component failure data were collected from IAEA technical documents or other reliable sources when available. Uncertainty and importance analyses have been performed. In addition to the failure rates obtained from external documents, the Safety Amplifier checkout procedures were incorporated into the effective repair rates, thus forming the complete model for the basic events of the fault tree. The cut-set analysis methodology was utilized in order to assure that the final results would be reasonably biased, i.e. conservative enough. For the same reason, only the reliability data with established bounds of confidence were used. The resulting reliability parameters indicate that the failures of the Safety Amplifier caused by external means may be much more frequent than those caused by random failures of the individual components.

™ FaultTree+ is a trademark of Isograph Ltd.

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